



Analysis of Algorithms Questions & Answers

Holger Findling
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Problem 1

What are the main differences between Analysis of Algorithms and Complexity Theory?
Is there a relationship between the two topics?
How does either topic help in the design and development of algorithms?

Problem 2

Besides merely being a finite set of rules that gives a sequence of operations for solving a specific type of problem, an algorithm has five important features. List the five features and provide a short explanation.

Problem 3

Suppose an array contains the following data: 5, 4, 7, 3, 2
Using the bubble sort algorithm, show the data in the array completing the first iteration through the outside loop.

Problem 4

Suppose an array contains the following data: 5, 4, 7, 3, 2
Using the selection sort algorithm, show the data in the array completing the first iteration through the outside loop.

Problem 5

Suppose an array contains the following data: 5, 4, 7, 3, 2
Using the insertion sort algorithm, show the data in the array completing the first iteration through the outside loop.

Problem 6

Show that $g(n) \in O(f(n))$
Where

$$g(n) = 2n^2 + 2n + 3$$

$$f(n) = 2n^3 + 2n + 3$$

Problem 7

Provide the terms of the sequence where $n = 7$ and $p = 2$

$$\begin{aligned} & n + p \\ & \sum_{k=1} \end{aligned}$$

Problem 8

Modify the Summation such that $k = 0$

$$\sum_{k=4}^{10} (5k - 2)$$

Problem 9

Solve for $S(n)$

$$S(n) = \sum_{k=1}^n (k + 3)$$

Problem 10

Perform a worst case analysis on the code snippet below.

```
const int n = 100;
int i = 0;
int x[n];
while (true) {
    if (i < n)
        x[i] = i++;
    else
        return;
}
```

Problem 11

Perform a worst case analysis on the code snippet below.

What are the values of x after the code executed, for $n = 2$ through 10?

```
int x = 0;
for (i = 0; i < n; i++) {
    for (j = 0; j < n; j++) {
        x += 1;
    }
}
```

Problem 12

Show the first 7 terms of the recurrence equation $T(n) = T(n-3) + T(n-2) + 2$

1	2	3				
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Problem 13

Perform a worst case analysis on the code snippet below.

What are the values of x after the code executed, for n = 2 through 10?

```
int x = 0;
for (i = 0; i < n; i++) {
    for (j = i; j < n; j++) {
        x += j;
    }
}
```

Problem 14

Provide the Time equation T (n).

Do not solve.

```
double Factorial (int n)
{
    if (n > 1)
        return (n * Factorial (n -1));
    return 1;
}
```

Problem 15

Using the expansion method solve $T(n) = 3T(n/3) + 3n$ for bigO.

Show all of your work!